

Digital SAT Math Mini Guide

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1 Tutorial: Basic Math for the SAT

This tutorial will cover the basic math skills you'll need to ace the SAT, including algebra, geometry, probability, and statistics. We'll also discuss useful calculator tips and tricks, and how to interpret graphs, charts, and tables.

1.1 Algebra for the SAT

Algebra is a fundamental component of the SAT Math section. A strong understanding of algebraic concepts will enable you to tackle a broad range of questions. Let's delve deeper into each concept you mentioned.

1.2 Solving Equations

Equations are mathematical statements that assert the equality of two expressions. To solve an equation means to find the values of the variable that make the equation true.

Example: Simplify $5(x - 2) + 3x = 20$.

First, distribute the 5 through the parentheses: $5x - 10 + 3x = 20$.

Combine like terms to simplify further: $8x - 10 = 20$.

Finally, solve for x by adding 10 to both sides, then dividing by 8: $x = \frac{20+10}{8} = \frac{30}{8} = 3.75$.

1.3 Linear Equations

A linear equation represents a straight line when graphed. The most common form of a linear equation is slope-intercept form, $y = mx + b$, where:

- m is the slope of the line, which represents the change in y for each unit change in x .
- b is the y -intercept, or the y -value where the line crosses the y -axis.

The slope between two points (x_1, y_1) and (x_2, y_2) is calculated as $\frac{y_2 - y_1}{x_2 - x_1}$.

Example: Given two points, $(2, 3)$ and $(4, 7)$, find the slope of the line passing through them.

The slope, m , would be $\frac{7-3}{4-2} = \frac{4}{2} = 2$.

1.4 Systems of Equations

A system of linear equations is a set of two or more linear equations that all contain the same set of variables. A solution to the system is a set of values for the variables that satisfies all the equations simultaneously. The two most common methods for solving systems of linear equations are substitution and elimination.

1. **Substitution:** Solve one of the equations for one variable in terms of the others, then substitute this expression into the other equations.

Example: Solve the system of equations $x + y = 6$ and $x - y = 2$ using substitution.

From the second equation, you can express x as $x = y + 2$. Substituting this into the first equation gives $(y + 2) + y = 6$, or $2y + 2 = 6$. Solving this gives $y = 2$ and substituting $y = 2$ into the second equation gives $x = 2 + 2 = 4$.

2. **Elimination:** Manipulate the equations so that adding or subtracting them eliminates one variable, making it possible to solve for the other variable.

Example: Solve the system of equations $x + y = 6$ and $x - y = 2$ using elimination.

If you subtract the second equation from the first, you eliminate y , leaving you with $2x = 4$, or $x = 2$. Substituting $x = 2$ into the first equation gives $2 + y = 6$, or $y = 4$.

Algebraic skills are essential for the SAT, so make sure to practice solving a variety of algebra problems. Once you have mastered these foundational concepts, you will be prepared

Sure, let's continue exploring more concepts in Algebra that are crucial for the SAT.

1.5 Quadratic Equations

A quadratic equation is a second-order polynomial equation in a single variable x , with a nonzero coefficient on x^2 . The general form is $ax^2 + bx + c = 0$.

Quadratic equations can be solved by factoring, completing the square, or using the quadratic formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$.

Example: Solve the quadratic equation $x^2 - 5x + 6 = 0$.

This equation can be factored to $(x - 2)(x - 3) = 0$. Setting each factor equal to zero gives the solutions $x = 2$ and $x = 3$.

1.6 Polynomials

A polynomial is an expression consisting of variables and coefficients, using only the operations of addition, subtraction, multiplication, and non-negative integer exponents.

Polynomials can be added, subtracted, multiplied, and divided. The degree of a polynomial is the highest power of the variable in the polynomial.

Example: Simplify the polynomial expression $(2x^2 - 3x + 1) + (x^2 + 2x - 1)$.

Adding like terms, we get $3x^2 - x + 2$.

1.7 Exponents and Radicals

Exponents are shorthand for repeated multiplication of the same thing. The number x^n means x multiplied by itself n times.

Radicals involve the use of the square root, cube root, and other roots. You can convert between radicals and exponents, as the n th root of a number is the same as raising that number to the power of $1/n$.

Example: Simplify $x^{\frac{2}{3}}$.

This is the same as the cube root of x^2 , often written as $\sqrt[3]{x^2}$.

1.8 Absolute Value

The absolute value of a number x , denoted by $|x|$, is the distance between x and zero on the number line. It is always non-negative. Absolute value equations often have two solutions.

Example: Solve the absolute value equation $|x - 2| = 5$.

This equation has two solutions: $x - 2 = 5$ gives $x = 7$ and $x - 2 = -5$ gives $x = -3$.

1.9 Functions

A function is a rule that assigns each input exactly one output. Functions are often represented as equations, tables, or graphs.

The SAT frequently tests understanding of function notation, such as $f(x) = 2x + 3$, and the concepts of domain and range.

Example: If $f(x) = 2x + 3$, find $f(5)$.

Substituting 5 for x gives $f(5) = 2(5) + 3 = 13$.

Algebra is a broad subject with many topics, but understanding these key areas will be very beneficial when tackling the SAT. Practice each of these topics to become more comfortable with their respective strategies and concepts.

Let's continue diving into more advanced topics in algebra which are often tested on the SAT.

1.10 Inequalities

An inequality is a relation between two expressions that may not be equal. Symbols used in inequalities include $<$ (less than), $>$ (greater than), \leq (less than or equal to), and \geq (greater than or equal to).

Solving inequalities generally follows the same procedures as solving equations, with one crucial difference: When you multiply or divide both sides of an inequality

by a negative number, you must reverse the inequality.

Example: Solve the inequality $-2x + 3 < 7$.

First, subtract 3 from both sides to get $-2x < 4$. Then divide both sides by -2 , remembering to flip the inequality, to get $x > -2$.

1.11 Rational Expressions and Equations

A rational expression is an expression that can be written as the quotient of two polynomials. A rational equation is an equation in which the variable appears in one or more rational expressions.

To solve a rational equation, first find a common denominator for all the terms, then multiply both sides of the equation by the common denominator to clear the fractions.

Example: Solve the rational equation $\frac{1}{x} + \frac{1}{x+1} = 1$.

Multiply through by the common denominator $x(x+1)$ to get $x+x+1 = x(x+1)$. Simplify to $2x+1 = x^2+x$, then rearrange to get the quadratic equation $x^2-x-1 = 0$. Solve this equation by factoring or using the quadratic formula.

1.12 Exponential and Logarithmic Functions

An exponential function is a function in which the variable is the exponent of a constant base. A logarithm is the inverse of an exponential function.

The SAT occasionally tests understanding of the laws of exponents and logarithms, as well as the ability to solve simple exponential and logarithmic equations.

Example: Solve the exponential equation $2^x = 8$.

Taking the logarithm base 2 of both sides, we get $x = \log_2 8 = 3$.

1.13 Sequences

A sequence is an ordered list of numbers. The SAT often tests understanding of arithmetic sequences (in which each term is a constant difference from the previous term) and geometric sequences (in which each term is a constant multiple of the previous term).

Example: If the fifth term of an arithmetic sequence is 12 and the tenth term is 22, find the fifteenth term.

The common difference is $(22 - 12)/(10 - 5) = 2$. Therefore, the fifteenth term is $22 + 2 \times (15 - 10) = 32$.

These are some of the more advanced algebra topics that are often tested on the SAT. The key to mastering these topics is practice. Work on problems in each of these areas until you feel comfortable with the concepts and methods.

2 Geometry for the SAT

Let's explore each of the key geometric concepts mentioned in more detail.

2.1 Triangles

Triangles are three-sided polygons, and they come in several varieties: equilateral, isosceles, scalene, right, acute, and obtuse.

1. **Equilateral triangles** have all sides of equal length, and all angles are 60 degrees.

2. **Isosceles triangles** have two sides of equal length. The angles opposite these sides are also equal.

3. **Scalene triangles** have no sides or angles that are equal.

4. **Right triangles** have one angle that is exactly 90 degrees. The side opposite this angle is called the hypotenuse. The other two sides are referred to as the "legs" of the triangle.

5. **Acute triangles** have all angles less than 90 degrees.
6. **Obtuse triangles** have one angle that is more than 90 degrees.

The sum of the interior angles in any triangle is always 180° .

A crucial concept involving right triangles is the Pythagorean Theorem, which states that $a^2 + b^2 = c^2$, where a and b are the lengths of the legs and c is the length of the hypotenuse.

Example: If one leg of a right triangle measures 3 units, the other leg measures 4 units, the hypotenuse should measure 5 units, because $3^2 + 4^2 = 9 + 16 = 25$, and the square root of 25 is 5.

2.2 Circles

A circle is a set of points in a plane that are all the same distance from a fixed point (the center). Some important properties and formulas associated with circles include:

1. **Diameter:** The longest distance across the circle, passing through the center.
2. **Radius:** The distance from the center to any point on the circle. It is half the length of the diameter.
3. **Circumference:** The distance around the circle. It is given by the formula $C = 2\pi r$ or $C = \pi d$, where r is the radius and d is the diameter.
4. **Area:** The number of square units that can fit inside the circle. It is given by the formula $A = \pi r^2$.
5. **Arc length:** The length of a portion of the circumference of the circle. It is usually given as a proportion of the entire circumference.
6. **Tangent line:** A line that touches the circle at exactly one point. This line is always perpendicular to the radius that intersects at that point.

2.3 Volume and Surface Area of 3D Shapes

Finally, understanding how to calculate the volume and surface area of various three-dimensional shapes is key for the SAT.

1. **Cylinder:** - Volume: $V = \pi r^2 h$, where r is the radius of the base and h is the height. - Surface Area: $A = 2\pi r h + 2\pi r^2$, where r is the radius and h is the height.

2. **Cone:** - Volume: $V = \frac{1}{3}\pi r^2 h$, where r is the radius of the base and h is the height. - Surface Area: $A = \pi r(r + l)$, where r is the radius and l is the slant height.

3. **Sphere:** - Volume: $V = \frac{4}{3}\pi r^3$, where r is the radius of the sphere. - Surface Area: $A = 4\pi r^2$, where r is the radius.

In addition to knowing these formulas, it's also crucial to understand the reasoning behind them. For instance, the formula for the volume of a cylinder can be derived by stacking an infinite number of infinitesimally thin circular discs, each of which has an area of πr^2 , to a height of h .

Example: If a cylinder has a radius of 2 units and a height of 3 units, its volume would be $V = \pi(2^2) \times 3 = 12\pi$ cubic units, and its surface area would be $A = 2\pi(2) \times 3 + 2\pi(2^2) = 12\pi + 8\pi = 20\pi$ square units.

The formulas for the volume and surface area of a cone and a sphere are more complex and typically require integral calculus to derive. However, you don't need to know how to derive these formulas for the SAT; you just need to be able to apply them.

Geometry is a rich field with many fascinating concepts, but the key topics we've discussed here—triangles, circles, and 3D shapes—will cover most of what you'll need to know for the SAT. Practice working with these shapes and their formulas until you feel comfortable, and you'll be well on your way to acing the geometry problems on the SAT.

Probability and Statistics

Understanding the basics of probability and statistics is key for the SAT.

Probability: Probability is calculated as the number of desired outcomes divided by the total number of outcomes. In independent events, the probabilities multiply.

Statistics: Be familiar with measures of central tendency (mean, median, mode) and spread (range, standard deviation). You should also understand how to interpret data from tables, graphs, and charts.

The total number of students is $30 + 20 + 15 + 35 = 100$. The number of students who prefer either pop or hip-hop music is $30 + 35 = 65$. Therefore, the percentage of students who prefer either pop or hip-hop is $\frac{65}{100} \times 100\% = 65\%$.

Probability Distributions

Sometimes, SAT problems will require you to understand simple probability distributions. For example, a problem may present a table listing outcomes of a random variable and their corresponding probabilities, and ask you to find the expected value.

The expected value is found by multiplying each outcome by its probability, then adding up these products.

Example: A game involves rolling a fair six-sided die. You win 2 if you roll a 1, 4 if you roll a 2, and lose 1 (that is, win -1) for any other roll. What is the expected value of this game?

The expected value is $E = (1) \left(\frac{1}{6}\right) \times 2 + (2) \left(\frac{1}{6}\right) \times 4 + (-1) \left(\frac{4}{6}\right) = \frac{1}{3} + \frac{4}{3} - \frac{4}{3} = \frac{1}{3}$ dollars.

This means that on average, you can expect to win about 33 cents per game.

Reading Graphs, Charts, and Tables for the SAT

In the SAT, you'll frequently encounter problems that involve interpreting data from visual displays, such as graphs, charts, and tables. Let's delve deeper into each of these elements and provide examples to solidify your understanding.

Percents and Proportions

Percents and proportions come up frequently on the SAT.

Percents: Understand how to convert between fractions, decimals, and percents. Be able to calculate percentages of quantities and changes in percentages.

Proportions: A proportion is an equation that states that two ratios are equivalent. Be comfortable solving problems that involve direct and inverse proportionality.

Quadratic Equations

Standard form: A quadratic equation is written as $ax^2 + bx + c = 0$.

Factoring: To solve quadratic equations, you often need to factor the equation. For example, the equation $x^2 - 5x + 6 = 0$ can be factored into $(x - 2)(x - 3) = 0$.

Quadratic formula: If a quadratic equation cannot be easily factored, use the quadratic formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$.

In summary, the key to success in SAT Math is a solid understanding of basic mathematical principles, combined with lots of practice. Don't rely too heavily on your calculator, and make sure you understand the underlying concepts, not just the formulas. Finally, remember to read each question carefully and pace yourself - it's not just about getting the right answer, but getting it in a timely manner. Good luck with your preparation!

Calculator Tips and Tricks for the SAT

The SAT permits the use of a calculator in certain sections, a tool that can greatly assist you when used correctly. Here are some tips and tricks to leverage the functionality of your calculator.

Know Your Calculator

It's essential to be familiar with the calculator you'll use on the test day. This means understanding how to perform basic operations (addition, subtraction, multiplication, division), but also knowing how to use more complex functions. This might include square roots, exponents, logarithms, trigonometric functions, and statistical functions. Each calculator model has unique ways of accessing and executing these functions, so make sure you know your device well.

Use for Complex Calculations

Your calculator is most useful for complex calculations that would be time-consuming to do by hand. This could include long divisions, operations with decimals, calculations involving square roots or exponents, and solving trigonometric problems. However, for simple arithmetic, it's often faster to solve the problem mentally or on paper.

Graphing Functions

If you're using a graphing calculator, it can be very beneficial for visualizing equations, exploring the shape of functions, or finding intersections of graphs. For instance, to solve a system of equations, you can graph each equation and find the point(s) where the graphs intersect. However, remember that not all problems will permit the use of a calculator, so it's important to know how to solve these problems algebraically as well.

Calculator Memory

Most calculators have a feature to store variables. This can be helpful for multi-step problems where you need to remember intermediate results. Learn how to store and recall variables on your calculator to make the most of this feature.

Check Your Work

If time permits, use your calculator to double-check your answers. This can help catch arithmetic errors or mistakes in calculation. However, be careful not to rush this step and inadvertently make additional mistakes.

Functions and Graphs

Understanding functions and graphs is an essential part of the SAT. Here's a brief overview of what you should know:

Functions

A function is a rule that assigns each input (or independent variable) to exactly one output (or dependent variable). You should understand the concept of a function, the difference between independent and dependent variables, and how to use function notation (like $f(x)$).

Graphs of Functions

You should be familiar with the shapes of basic function graphs. These include linear functions ($y = mx + b$), quadratic functions ($y = ax^2 + bx + c$), and absolute value functions ($y = |x|$). Moreover, you should recognize how transformations affect the graphs of these functions. For instance, know what happens to the graph of $y = f(x)$ when it changes to $y = f(x) + c$, $y = f(x - c)$, $y = cf(x)$, and $y = f(cx)$.

Solving Equations Graphically

In many cases, graphs can help solve equations. The x-intercepts of the graph of a function (the points where the graph crosses the x-axis) represent the solutions to the equation obtained by setting the function equal to zero. Understanding this concept can aid in finding solutions to equations quickly.

As always, practice makes perfect. Work through many problems involving calculator use, functions, and graphs to become comfortable with these concepts. Best of luck with your SAT preparation!

Trigonometry for the SAT

Trigonometry might not constitute a large part of the SAT, but understanding basic trigonometric principles can indeed provide you with a few additional points. Let's

delve into the basics.

Basic Ratios: Sine, Cosine, Tangent

The three basic trigonometric ratios—sine, cosine, and tangent—are often remembered using the acronym SOHCAHTOA:

- *Sine* (SOH): Sine of an angle in a right triangle is the ratio of the length of the side that is opposite that angle to the length of the longest side of the triangle (the hypotenuse). Symbolically, $\sin \theta = \frac{\text{Opposite}}{\text{Hypotenuse}}$.

- *Cosine* (CAH): Cosine of an angle in a right triangle is the ratio of the length of the side that is adjacent to (i.e., next to) that angle to the length of the hypotenuse. Symbolically, $\cos \theta = \frac{\text{Adjacent}}{\text{Hypotenuse}}$.

- *Tangent* (TOA): Tangent of an angle in a right triangle is the ratio of the sine of the angle to the cosine of the angle. This is the same as the ratio of the side opposite the angle to the side adjacent. Symbolically, $\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$.

Special Triangles: 30-60-90 and 45-45-90

Two special right triangles frequently show up in SAT problems: the 30-60-90 triangle and the 45-45-90 triangle. These triangles have angles of 30 degrees, 60 degrees, and 90 degrees, or 45 degrees, 45 degrees, and 90 degrees, respectively. What makes them special are their side lengths, which are always in a certain ratio.

In a 30-60-90 triangle, the side lengths are in the ratio $1 : \sqrt{3} : 2$. The side opposite the 30-degree angle is half the length of the hypotenuse, and the side opposite the 60-degree angle is $\sqrt{3}$ times the length of the side opposite the 30-degree angle.

In a 45-45-90 triangle, the side lengths are in the ratio $1 : 1 : \sqrt{2}$. The two legs are the same length, and the hypotenuse is $\sqrt{2}$ times the length of a leg.

Trigonometric Graphs: Sine, Cosine, Tangent

Lastly, it would be beneficial to recognize the basic shapes of the graphs of sine, cosine, and tangent functions:

- *Sine* ($y = \sin x$): The graph of the sine function is a smooth, continuous wave that oscillates above and below the x-axis, reaching a maximum height of 1 and a minimum height of -1.

- *Cosine* ($y = \cos x$): The graph of the cosine function is also a smooth wave. It looks much like the sine wave but is shifted to the left by 90 degrees, or $\frac{\pi}{2}$ radians.

- *Tangent* ($y = \tan x$): The graph of the tangent function is different. It consists of vertical asymptotes (lines that the graph gets infinitely close to but never touches) at the points where cosine equals zero.

Mastering these topics in trigonometry will make solving any trig-related question on the SAT much easier. As with all topics, practice is crucial, so be sure to find and solve plenty of trigonometry practice problems. Good luck with your SAT preparation!

3 Word Problems for the SAT

Word problems frequently appear on the SAT, often presenting real-world scenarios. They require you to interpret the language of the problem, translate English sentences into mathematical equations, and use reasoning skills to solve them. Here are some useful tips and tricks to tackle these problems.

3.1 Setting up Equations

Careful reading is paramount. Start by identifying what the question is asking for. Are you being asked to find a specific quantity or determine a relationship between variables?

Next, try to convert the language of the problem into a mathematical format. This process might involve identifying variables (the unknowns), constants (the known values), and the relationships between them, which often come in the form of equations. Let's consider an example:

"Sarah has twice as many books as Tom. Together, they have 18 books. How many books does each person have?"

In this case, we can let T represent the number of books Tom has and S represent the number of books Sarah has. We know two things from the problem:

1. Sarah has twice as many books as Tom, which gives us $S = 2T$. 2. Together, they have 18 books, which gives us $S + T = 18$.

We now have a system of two equations that we can solve to find the number of

books each person has.

3.2 Units

Word problems often involve quantities with units, such as time, distance, or money. It's crucial to make sure that all quantities in your equations are in the same units. If they aren't, you'll need to convert them.

For example, if you're given a speed in miles per hour and a time in minutes, you might need to convert the time to hours or the speed to miles per minute, depending on what the question is asking.

3.3 Reasoning

After you've found a solution, take a moment to check if it makes sense in the context of the problem. If the problem involves a real-world situation, your answer should be reasonable within that context.

For instance, in our books example, if we ended up with a negative number of books or a fractional number of books, we would know that something went wrong, as you can't have negative or fractional books.

Remember, while the language used in word problems can often seem complex and tricky, the underlying mathematics is typically straightforward. Practice is key to becoming proficient at translating the language of word problems into the language of mathematics.

4 Percents

Percents are another topic that shows up frequently in SAT word problems.

Here's a quick refresher on some of the key concepts:

- To convert a percent to a decimal, divide by 100. For example, 50% becomes 0.50.
- To convert a decimal to a percent, multiply by 100. For example, 0.75

becomes 75%. - To find the percent of a number, multiply the number by the percent (in decimal form). For example, 20% of 50 is $0.20 \times 50 = 10$.

Let's apply these concepts in a typical SAT-style word problem:

"A store is having a 25% off sale on a pair of shoes that originally cost \$80. What is the sale price?"

In this problem, we're asked to find the sale price after a 25% discount. First, we need to find the amount of the discount, which is 25% of \$80: $0.25 \times 80 = 20$. The sale price is then the original price minus the discount: $\$80 - \$20 = \$60$.

5 Ratios

Ratios express the relationship between two quantities. They can be written in several forms, such as "3 to 4", "3:4", or " $\frac{3}{4}$ ".

A key concept with ratios is that they can be scaled up or down by multiplying or dividing both quantities by the same number. For example, if the ratio of dogs to cats in a park is 3:4 and there are 12 dogs, then there are $4 \times (12 \div 3) = 16$ cats.

Here's an example of a ratio problem you might see on the SAT:

"In a classroom, the ratio of boys to girls is 3:2. If there are 15 boys, how many girls are there?"

To solve this problem, you can scale up the ratio by multiplying both parts by 5 (since $15 \div 3 = 5$), which gives you the number of girls: $2 \times 5 = 10$.

Remember, practice is the key to mastering these concepts. The more problems you solve, the more comfortable you'll become with these kinds of questions on the SAT.

6 Exponents and Radicals for the SAT

Exponents and radicals are used frequently in the SAT math section, and understanding them is crucial to performing well on the exam.

6.1 Laws of Exponents

Exponents are a shorthand way to express repeated multiplication. The number being multiplied is the base, and the number of times it's being multiplied is the exponent. For example, $2^3 = 2 \times 2 \times 2 = 8$.

There are several important rules of exponents you should know:

- **Product of powers rule:** $a^n \cdot a^m = a^{n+m}$. When you multiply two powers with the same base, you add the exponents.

Example: $2^3 \cdot 2^4 = 2^{3+4} = 2^7 = 128$.

- **Power of a power rule:** $(a^n)^m = a^{nm}$. When you raise a power to a power, you multiply the exponents.

Example: $(3^2)^4 = 3^{2 \times 4} = 3^8 = 6561$.

- **Quotient of powers rule:** $a^n / a^m = a^{n-m}$. When you divide two powers with the same base, you subtract the exponents.

Example: $10^5 / 10^2 = 10^{5-2} = 10^3 = 1000$.

6.2 Radicals

Radicals, or roots, are the opposite of exponents. While an exponent tells you how many times to multiply a number by itself, a radical tells you to find which number, when multiplied by itself a certain number of times, gives you the original number. The most commonly encountered radical is the square root. For example, the square root of 9 is 3, because $3^2 = 9$.

Radical expressions can often be simplified by finding factors of the number under the radical that are perfect squares (for square roots), perfect cubes (for cube roots), etc.

Example: $\sqrt{50} = \sqrt{25 \times 2} = \sqrt{25} \times \sqrt{2} = 5\sqrt{2}$.

6.3 Negative and Fractional Exponents

Negative exponents represent the reciprocal of the base raised to the corresponding positive exponent. That is, $a^{-n} = 1/a^n$.

Example: $5^{-2} = 1/5^2 = 1/25 = 0.04$.

Fractional exponents represent roots. The numerator of the fraction is the power, and the denominator is the root. So, $a^{1/n}$ is the n -th root of a , and $a^{m/n} = (a^m)^{1/n}$.

Example: $16^{1/2} = \sqrt{16} = 4$ and $8^{2/3} = (8^2)^{1/3} = \sqrt[3]{64} = 4$.

Understanding and being comfortable with these rules will allow you to tackle a variety of problems on the SAT involving exponents and radicals. As always, practice is key to becoming proficient in these concepts.

7 Mental Math Tricks to Speed up SAT Problem Solving

Developing strong mental math skills can significantly improve your speed and efficiency when solving problems on the SAT. In this tutorial, we'll explore some helpful mental math tricks to help you tackle math problems more quickly. Practice these strategies regularly to enhance your mental math abilities.

7.1 Estimation and Rounding

Estimation allows you to quickly approximate the value of numbers. By rounding numbers to the nearest whole number or a simpler value, you can simplify calculations and arrive at a reasonably accurate answer more rapidly.

For example, if you encounter a multiplication problem like 36×7 , you can round both numbers to the nearest ten, resulting in $40 \times 10 = 400$. This estimation can help you eliminate answer choices or quickly estimate the magnitude of the answer.

7.2 Breaking Numbers Apart

Breaking down numbers into more manageable components can simplify calculations. Look for numbers that can be split into smaller, easier-to-work-with parts.

For instance, if you encounter 36×25 , you can break down 36 into 30 and 6, and then multiply each part separately: $(30 \times 25) + (6 \times 25) = 750 + 150 = 900$.

7.3 Multiplying by Powers of 10

When multiplying numbers by powers of 10 (such as 10, 100, or 1000), you can use a shortcut to quickly determine the result. Simply move the decimal point to the right by the same number of zeros as the power of 10.

For example, if you need to calculate 75×100 , instead of performing the multiplication, you can move the decimal point two places to the right, resulting in 7500.

7.4 Percentage Calculations

Working with percentages efficiently is crucial for many SAT problems. Familiarize yourself with common percentage conversions to speed up calculations.

For example, to find 10% of a number, divide it by 10. To find 25%, divide it by 4. To find 50%, divide it by 2. These quick calculations can be useful for estimating or solving problems that involve percentages.

7.5 Recognizing Patterns and Shortcut Formulas

Look for patterns and formulas that can expedite calculations. For instance, familiarize yourself with the squares of numbers up to 20 and common geometric formulas.

For example, if you encounter a problem involving calculating the area of a rectangle with sides of lengths 12 and 8, instead of multiplying, recognize that it's simply $12 \times 8 = 96$.

7.6 Mental Division

Develop mental division skills by practicing dividing numbers mentally. Focus on recognizing division patterns and using known facts to simplify calculations.

For example, if you need to divide $140 \div 7$, recognize that both numbers are divisible by 7, resulting in 20.

7.7 Utilizing Symmetry and Equalities

Exploit symmetry and equalities in math problems. Look for ways to transform the problem or equation to simplify calculations.

For instance, if you encounter a problem involving subtracting two similar numbers, such as $367 - 363$, recognize that the difference will be the same as subtracting the difference between the numbers from the larger number: $(367 - 360) - 3 = 7 - 3 = 4$.

7.8 Practicing Mental Math Regularly

The key to improving your mental math skills is regular practice. Dedicate time to solve math problems mentally, challenge yourself with mental math exercises, and attempt mental calculations in your daily life.

Studying for the SAT Math section may seem daunting, but with a solid understanding of these basic concepts and plenty of practice, you'll be well on your way to a high score. Remember to pace yourself during the test and to carefully read each question before beginning your work. Good luck!